SOFTWARE & TECH

What Is An Interval In Math

PUBLISHED
November 25, 2026

REFERENCE
#1795583736821012

Introduction

If you have ever worked with graphs, solved inequalities, or studied calculus, you have encountered the concept of an interval. An interval is one of the most fundamental building blocks in mathematics, especially in algebra, analysis, and geometry. It represents a continuous range of numbers between a starting point and an ending point. Understanding what an interval is and how to use it is essential for expressing solution sets, describing domains and ranges of functions, and performing operations on sets of real numbers.

In this article, we will explore the definition of an interval, the different types of intervals, how to write them using interval notation, and why they are so important in math. Whether you are a student brushing up on precalculus or someone looking to refresh your math fundamentals, this guide will give you a clear and thorough understanding of intervals.

Understanding the Concept of an Interval

Definition and Basic Notation

In mathematics, an interval is a set of real numbers that includes every number between two given endpoints. The endpoints themselves may or may not be part of the interval. The simplest way to think about an interval is as a contiguous segment of the number line. For example, all numbers from 2 to 5, including 2 and 5, form an interval. If we exclude the endpoints, we still have an interval, but it is considered open at those boundaries.

Interval notation is a shorthand way of writing intervals. Instead of listing numbers, we use parentheses and brackets to indicate whether endpoints are included or excluded. A bracket **[** or **]** means the endpoint is included (closed), while a parenthesis **(** or **)** means the endpoint is excluded (open). For instance, the interval of all numbers from 2 to 5 including both endpoints is written as **[2, 5]**. If we exclude both endpoints, we write **(2, 5)** . A mix, such as including 2 but not 5, is written as **[2, 5)**.

Why Intervals Matter in Mathematics

Intervals are everywhere in math. When you solve an inequality like *x* > 3, the solution is an interval: all numbers greater than 3, written as **(3, ".)**When you study functions, the domain is often an interval or a union of intervals. In calculus, intervals are used to define continuity, intervals of increase or decrease, and integration limits. Without intervals, describing continuous ranges of numbers would be cumbersome. They provide a precise and efficient language for communicating mathematical ideas.

Types of Intervals

There are four main types of intervals, categorized by whether the endpoints are included and whether the interval extends to infinity.

Closed Intervals [a, b]

A closed interval includes both endpoints. It contains every real number from *a* to *b* inclusive. Notation: **[a, b]**. For example, **[0, 1]** includes 0, 1, and every number in between. In set-builder notation: {*x* | *a* "d "*b*}. Closed intervals are used when the endpoints are part of the solution set, such as when an inequality has a "less than or equal to" sign.

Open Intervals (a, b)

An open interval excludes both endpoints. It contains all numbers between *a* and *b* but not *a* or *b* themselves. Notation: **(a, b)**. Example: **(0, 1)** includes 0.5, 0.999, but not 0 or 1. Set-builder: {*x* | *a* < *x* < *b*}. Open intervals appear in strict inequalities like *x* > 2 and *x* < 5, which together form (2, 5).

Half-Open (or Half-Closed) Intervals

These intervals include one endpoint but not the other. There are two possibilities:

- [a, b) : includes a, excludes b. Example: [3, 7) contains 3, 3.5, 6.999, but not 7.
- (a, b] : excludes a, includes b. Example: (" 1, 4] contains all numbers greater than " 1 up to and including 4, but not " 1 itself.

Half-open intervals often arise when one boundary is included due to an "or equal" condition while the other is strict.

Infinite Intervals

When an interval has no upper bound or no lower bound, we use the infinity symbols " or ". Infinity is always accompanied by a parenthesis because it is a concept, not a number, and cannot be included.

- (a, ") : all numbers greater than a. Example: (0, ") means all positive real numbers.
- [a, ") : all numbers greater than or equal to a. Example: [" 2, ").
- (" , b) : all numbers less than b.
- (" , b] : all numbers less than or equal to b.
- (" , ") : the entire set of real numbers.

Infinite intervals are crucial for describing unbounded domains and ranges.

Visualizing Intervals on a Number Line

A number line is the best tool to visualize intervals. Draw a horizontal line with marks for endpoints. For a closed endpoint, draw a solid dot (or filled circle). For an open endpoint, draw a hollow circle. Then shade the region between them. For infinite intervals, extend the shading with an arrow to indicate it continues forever.

For example, the interval **[" 1, 3)** would show a solid dot at " 1, a hollow circle at 3, and a shaded line from " 1 to 3. This visual representation makes it easy to see what numbers are included and helps avoid mistakes when working with unions or intersections of intervals.

Interval Notation and Set-Builder Notation

Two common ways to describe sets of numbers are interval notation and set-builder notation. Interval notation is concise; set-builder is more descriptive. For the set of all numbers between 2 and 5, inclusive of 2 but not 5:

- Interval notation: [2, 5)
- Set-builder notation: {x | 2 "d x < 5}

Learning to convert between these two forms is a key skill in algebra. Set-builder notation can express intervals that are not contiguous (e.g., all integers between 2 and 5), but for real numbers, intervals are the standard.

Operations on Intervals

Intervals can be combined using set operations: union, intersection, and difference. These are especially useful when solving compound inequalities or describing piecewise functions.

Union of Intervals

The union of two intervals contains all numbers that belong to either interval. Symbol: "*. For example, the union of (1, 3] and [4, 6) is written as **(1, 3] "* [4, 6)**On a number line, you shade both regions. The union can also connect intervals that are separated by a gap.

Intersection of Intervals

The intersection of two intervals contains only numbers that are in both intervals. Symbol: "). For example, [0, 5] ") (2, 7) = (2, 5]. To find the intersection, identify the overlapping region. If intervals do not overlap, the intersection is empty, denoted by " .

Difference of Intervals

The difference (or set minus) of intervals, written as *A "B*, consists of numbers in *A* that are not in *B*. For instance, [0, 10) " (3, 5) = [0, 3] "* [5, 10). Computing differences can involve splitting intervals at the boundaries.

Real-World Applications of Intervals

Intervals are not just abstract math – they appear in many real-life contexts. In engineering, tolerance ranges for measurements are intervals, e.g., a bolt diameter of 5mm ± 0.1mm translates to [4.9, 5.1]. In physics, time intervals describe periods of motion. In statistics, confidence intervals estimate population parameters. In computer science, intervals are used in algorithms for scheduling, data analysis, and interval arithmetic.

For example, when a weather forecast says "temperatures between 20°C and 25°C," that is an interval [20, 25]. When a company expects sales in a quarter to be between $1 million and $1.5 million, that is an interval. Understanding intervals helps in interpreting data ranges and making decisions based on boundaries.

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